MATH 141, Fall 2025, Nathan Reading

Review: Test 3 (and beyond)

This is an overview of the most important skills and understanding I expect you to have developed. I don't promise that every exam problem will match with something on this sheet.

Exam questions might test your understanding of some of the following important terms and concepts:

summation notation antiderivative indefinite integral definite integral The Fundamental Theorem of Calculus

The exam might reasonably test your ability to carry out some of the following procedures.

- Use l'Hôpital's Rule (perhaps more than once) to evaluate a limit. Specifically, use l'Hôpital's Rule directly on one of the indeterminate forms  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$  or rewrite a limit of indeterminate form  $0 \cdot \infty$ ,  $\infty \infty$ ,  $0^0$ ,  $1^\infty$  or  $\infty^0$  as a limit of indeterminate form  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , then use l'Hôpital's. You might not be told what indeterminate form is given and you might be asked to identify what indeterminate form is given.
- Compute an indefinite integral by finding an antiderivative. (This is a pretty general question, and includes some of the later questions.)
- Approximate\* a definite integral as a right Riemann sum.
- Compute\* a definite integral by computing (positive and negative) areas directly.
- Compute\* a definite integral using the basic properties of definite integrals.
- Compute a derivative using the Fundamental Theorem of Calculus (Part 1).
- Compute\* a definite integral using the Fundamental Theorem of Calculus (Part 2). (Again, this is a pretty general question, and includes some of the later questions.)
- Compute an integral (indefinite or definite) using basic derivative facts\*\*.
- Compute an integral (indefinite or definite) using substitution\*\*.
- Compute an integral (indefinite or definite) using integration by parts\*\*.

I may ask a few challenge questions at the end of the exam, worth very few points, and these problems are exempt from anything I have told you or will tell you about what I will or will not ask on the test.

Closed book, closed notes, no calculators.

## The following additional types of problems will not be on Test 3, but will be on the final:

- Find the area bounded by given curves.
- Find the volume of a solid of revolution using one of the following methods:
  - the "discs" method.
  - the "washers" method.
  - the "shells" method.

You might not be told which of the three methods to use.

<sup>\*</sup>In all of these problems, please make sure you know whether you are being asked to compute or to approximate a definite integral.

<sup>\*\*</sup>You might not be told whether substitution, parts, or neither is needed.