MATH 141 Fall 2025, QUIZ 4

1. Find the derivative f'(x) of each given function:

a.
$$f(x) = 4x^2 - 5$$

e.
$$f(x) = 3\sin x - 4\cos x$$

b.
$$f(x) = (4x^2 - 5)(3x^4 + x^3 - 7x + 1)$$

f.
$$f(x) = x^4 \sin x$$

c.
$$f(x) = \sqrt[3]{x} + 5\sqrt{x}$$

g.
$$f(x) = \frac{\sin x + 1}{\cos x}$$

d.
$$f(x) = \frac{x^2 + 4x}{x^3 - 5x + 1}$$

h.
$$f(x) = \cos(x + \sqrt{x})$$

i.
$$f(x) = \sin(\sin(\sin x))$$

- 2. Find the derivative of $f(x) = \sin^2 x + \cos^2 x$, but do it twice. The first time, forget *all* trig identities and find the derivative using differentiation rules. The second time, use the-trig-identity-that-everyone-must-simply-know to rewrite f(x), and then use the simplest of all differentiation rules.
- 3. Let $f(x) = (x^2 1)^6$. Find all points where the tangent line to f(x) is horizontal. (Give both the x-coordinate and the y-coordinate of each point.)